



## Resilience of critical infrastructure exercises

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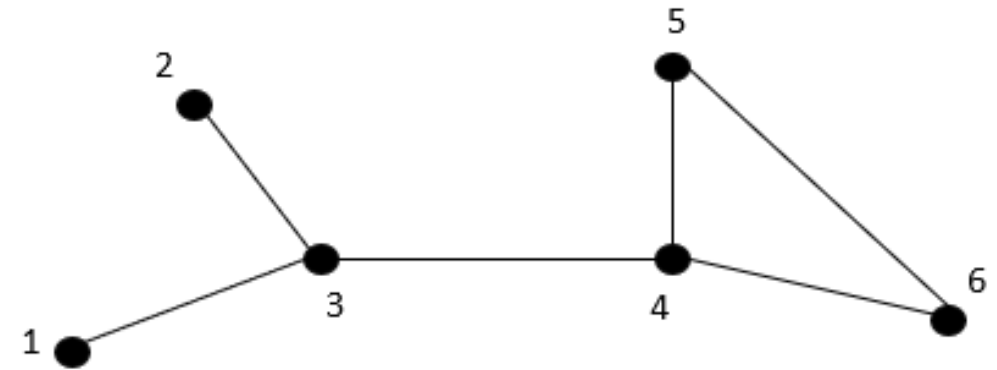


## Exercise 4

### Centrality Measures

2

In the following network, find the topological centrality measurements ( $C_i^D$ ,  $C_i^C$ ,  $C_i^B$  and  $C_i^I$ ) of node 3.





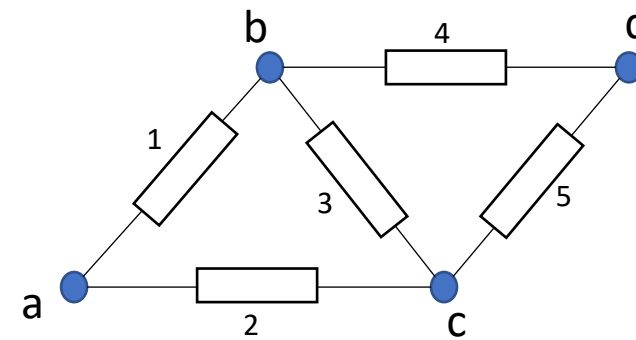
## Exercise 5-D Complexity Measurement

3

Consider the following network system. All the components have equal failure rate  $\lambda = 10^{-4} \text{ days}^{-1}$ .

The system fails when there is no connection between node a and node d.

Find the vulnerability index of the network due to the disconnection of link **bc**.

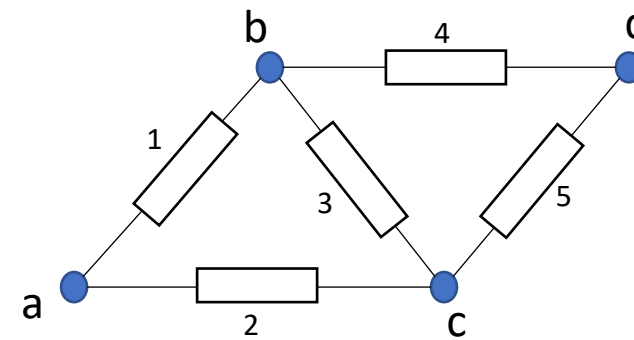




Consider the following network system. All the components have equal failure rate  $\lambda = 10^{-4} \text{ days}^{-1}$ .

The system fails when there is no connection between node a and node d.

- Considering the failure rate for node c as  $5 \times 10^{-4} \text{ h}^{-1}$ , draw the Goal Tree Success Tree for the top goal “receiving signal successfully to d”.
- Compute the probability of the top goal for one month.

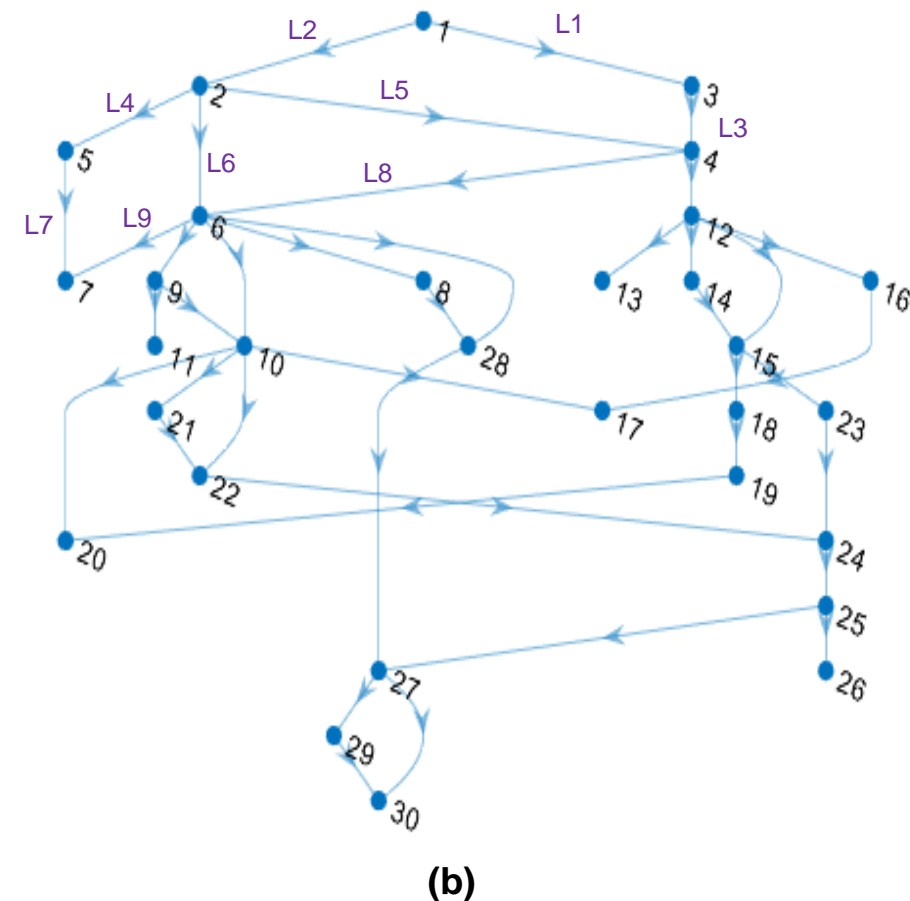
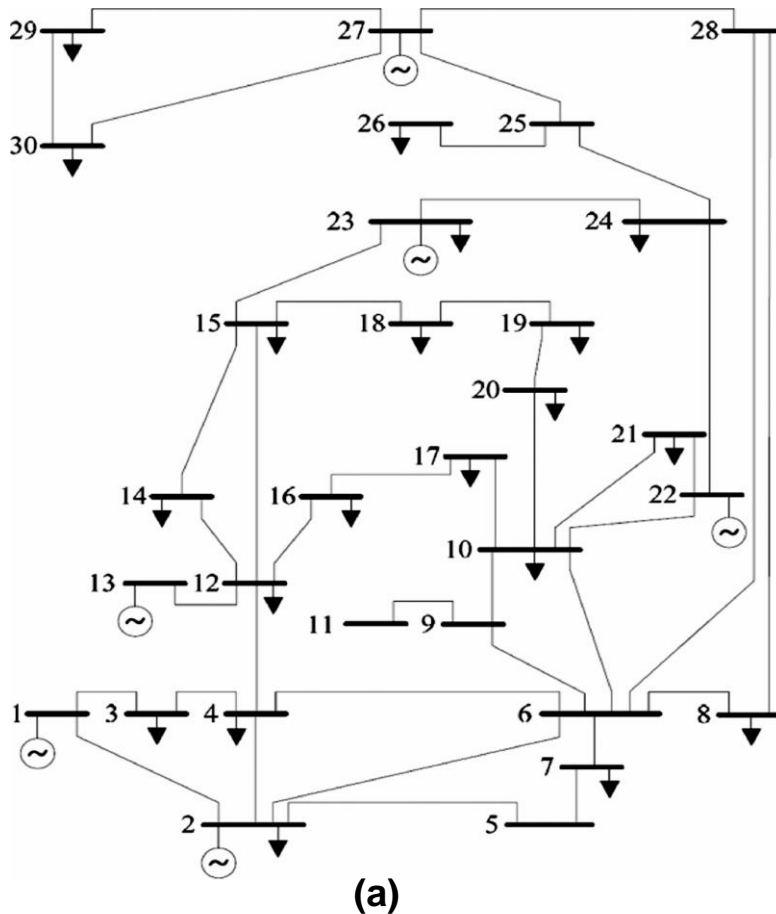




## IEEE30 Bus Power Distribution System

The standard IEEE30 power distribution system is shown in the figure (a). Only the major components are to be considered: the Generators (6 generators), Loads (20 loads) and power delivery paths consisting of lines (L) and buses (B). The stochastic network is shown in figure (b).

Draw a GTST for supplying power successfully to Load 4.





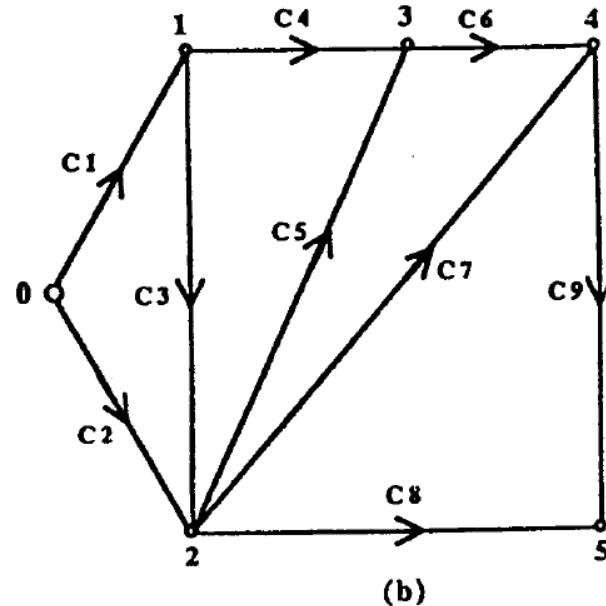
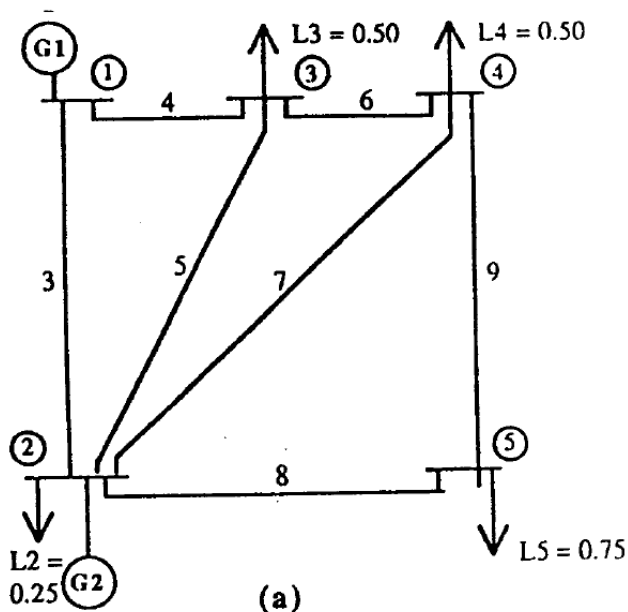
## Exercise 7 Resilience Metrics

6

Fig. (a) shows a 5-bus system with two generators at node 1 and 2 and four load at node 2, 3, 4 and 5. The orientation of power flow in the network is shown in Fig. (b) and system operating data are given in the following table.

System performance  $P(t)$  is defined based on the cumulative power flow delivered to the loads.

At  $t_0 = 2$  a disruption happens and leads to immediate disconnection of node 2 and its failure to supply power. Node 2 is fixed at  $t_r = 10$ , and maximum acceptable system recovery instant is  $t^* = 14$ . If we assume that node 2 connects at  $t_r$  but it takes  $\Delta t_r = 1$  for successor nodes and loads to connect to node 2, find the resilience metric 1 (Henry), 2 (Zobel) and 3 (Bruneau) for system operation.



Element	Capacity of element (C)
1	1.5
2	0.50
3	1
4	0.5
5	0.25
6	0.25
7	0.50
8	0.75
9	0.25



# THANK YOU

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